# 3D Line Mapping Revisited 

THU-PM-080
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## Robust Scalable Pipeline for Mapping 3D Lines



## Examples of Our 3D Line Maps



## Opening up new possibilities to multiple applications

## Example: Hybrid Localization

before optimization
after optimization

| Dataset | HLoc* | PtLine | Ours |
| :--- | :---: | :---: | :---: |
| Cambridge | $7.0 / 0.13 / 44.0$ | $7.4 / 0.13 / 43.5$ | $\mathbf{6 . 7} / \mathbf{0 . 1 2} / \mathbf{4 6 . 1}$ |
| 7Scenes | $3.3 / 1.08 / 73.0$ | $3.3 / 1.09 / 72.7$ | $\mathbf{3 . 0} / \mathbf{1 . 0 0} / \mathbf{7 8 . 0}$ |
| Dataset | HLoc* w/ Depth | PtLine | Ours w/ Depth |
| 7Scenes w/ depth | $2.9 / 0.94 / 80.1$ | $2.8 / 0.93 / 80.6$ | $\mathbf{2 . 6} / \mathbf{0 . 8 7} / \mathbf{8 3 . 5}$ |


point-alone localization
hybrid point-line localization

|  | (T / R) err. $\downarrow$ | Acc. $\uparrow$ |
| :--- | :---: | :---: |
| HLoc* | $5.2 / 1.46$ | 46.8 |
| HLoc* w/ depth | $4.7 / 1.25$ | 53.4 |
| PtLine | $4.8 / 1.33$ | 51.9 |
| Ours w/L3D++ | $4.1 / 1.14$ | 60.8 |
| Ours w/ LIMAP | $\mathbf{3 . 7} / \mathbf{1 . 0 2}$ | $\mathbf{7 1 . 1}$ |

Example: Hybrid Bundle Adjustment

|  | Med. error $\downarrow$ | AUC @ $\left(1^{\circ} / 3^{\circ} / 5^{\circ}\right) \uparrow$ |
| :--- | :---: | :---: |
| COLMAP | 0.188 | $77.3 / 89.0 / 91.6$ |
| COLMAP + LIMAP refinement | $\mathbf{0 . 1 4 6}$ | $\mathbf{8 2 . 9 / 9 1 . 2 / 9 3 . 0}$ |



# Open-sourcing - LIMAP: a toolbox for mapping and localization with line features 




Snavely et al. Bundler (2010)

COLMAP


Schönberger et al. COLMAP (2016)

Modern multi-view geometry software heavily rely on feature points.

## What is missing from the 3D point map?



SuperPoint + COLMAP point triangulator


Line Mapping


Point-line Association


Parallelism \& Orthogonality


Von Gioi et al. LSD: A fast line segment detector with a false detection control (2010)


Zhou et al. LCNN (2019)


Pautrat et al. SOLD2 (2021)

## Challenges on mapping lines

- Inconsistent endpoints
- Line Fragmentation
- No Two-view Geometric Verification
- Weak matchers
- Degenerate Configurations
$\qquad$


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## Algebraic Line triangulation

Ray-plane intersection on both endpoints respectively
Degeneracy happens when ray lies on the plane! 0 / 1 / 2 degenerate endpoints


Blue - degree 1
red - degree 2
black degree >= 3

0 degree - isolated point

1 degree - point lying on the line

>=2 degree - line-line intersection

## A brief overview of our mapping pipeline



Also easily extends with available depth maps if applicable.


## Triangulating proposals



Using shared neighboring 3D points to help avoid degeneracy!

## Scoring each proposal \& Building tracks



## Joint Optimization over Points, Lines and VPs

- Reprojection error
- Point-line associations
- Line-line associations via VP (construct VP tracks in advance)

Weighted by analyzing connections from 2D relational graphs inside the track

Plücker coordinates!




Local planes from degree-2 junctions


VP detection
VP track visualization (vertical)


Input
Ours







## We do have quantitative evaluation

- Length Recall at certain threshold
- Precision at certain threshold
- Average number of image support / average number of line support

| Line type | Method | R1 | R5 | R10 | P1 | P5 | P10 | \# supports |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| LSD | L3D++ | 37.0 | 153.1 | 218.8 | 53.1 | 80.8 | $\mathbf{9 0 . 6}$ | $(14.8 / 16.8)$ |
|  | ELSR | 13.9 | 59.7 | 96.5 | 55.4 | 72.6 | 82.2 | (N/A / N/A) |
|  | Ours | $\mathbf{4 8 . 6}$ | $\mathbf{1 8 5 . 2}$ | $\mathbf{2 5 1 . 3}$ | $\mathbf{6 0 . 1}$ | $\mathbf{8 2 . 4}$ | 90.0 | $(\mathbf{1 6 . 4} / \mathbf{2 0 . 5})$ |
| SOLD2 | L3D++ | 36.9 | 107.5 | 132.8 | 67.2 | $\mathbf{8 6 . 8}$ | $\mathbf{9 3 . 2}$ | $(13.2 / 20.4)$ |
|  | Ours | $\mathbf{5 4 . 3}$ | $\mathbf{1 5 1 . 1}$ | $\mathbf{1 9 1 . 2}$ | $\mathbf{6 9 . 8}$ | 84.6 | 90.0 | $(\mathbf{1 6 . 5} / \mathbf{3 8 . 7})$ |
|  |  |  |  |  |  |  |  |  |
| Method |  | R5 | R10 | R50 | P5 | P10 | P50 | \# supports |
|  | 373.7 | 831.6 | 2783.6 | 40.6 | 54.5 | 85.9 | $(8.8 / 9.3)$ |  |
| ELSR | 139.2 | 322.5 | 1308.0 | 38.5 | 48.0 | 74.5 | (N/A / N/A) |  |
| Ours (line-only) | 472.1 | 1058.8 | 3720.7 | $\mathbf{4 6 . 8}$ | $\mathbf{5 8 . 4}$ | $\mathbf{8 6 . 1}$ | $(10.3 / 11.8)$ |  |
| Ours | $\mathbf{5 0 8 . 3}$ | $\mathbf{1 1 5 4 . 5}$ | $\mathbf{4 1 7 9 . 5}$ | 46.0 | 56.9 | 83.7 | $(\mathbf{1 0 . 4} / \mathbf{1 2 . 0})$ |  |

> Vp-Line Association
> Aachen database (6697 images)

## Old saying: Every road line leads to Rome



## Scalable to Rome 16k




British Museum from [47]


Piazza San Marco from [47]






4iv

London Bridge from [47]

$\triangle D \Delta \Delta D_{0}$



St. Paul's Cathedral from [47]


Courtroom (indoor and outdoor) from [26]


Lighthouse from [26]


Truck from [26]


Museum from [26]

$\nabla^{\nabla}$
Train from [26]


Temple from [26]

## Localization



Before optimization


After optimization

## Hybrid localization with points and lines



Point-alone localization with HLoc


Hybrid localization with 4 solvers

| Scene | HLoc | PtLine | Ours |
| :--- | :---: | :---: | :---: |
| Great Court | $\mathbf{9 . 5} / \mathbf{0 . 0 5} / \mathbf{2 0 . 4}$ | $11.2 / 0.07 / 17.8$ | $9.6 / \mathbf{0 . 0 5} / 20.3$ |
| King's College | $6.4 / \mathbf{0 . 1 0} / 37.0$ | $6.5 / \mathbf{0 . 1 0} / 37.0$ | $\mathbf{6 . 2} / \mathbf{0 . 1 0} / \mathbf{3 9 . 4}$ |
| Old Hospital | $12.5 / 0.23 / 22.5$ | $12.7 / 0.24 / 20.9$ | $\mathbf{1 1 . 3} / \mathbf{0 . 2 2} / \mathbf{2 5 . 4}$ |
| Shop Facade | $2.9 / 0.14 / 78.6$ | $\mathbf{2 . 7} / \mathbf{0 . 1 2 / 7 9 . 6}$ | $\mathbf{2 . 7} / 0.13 / \mathbf{8 1 . 6}$ |
| St Mary's Church | $\mathbf{3 . 7} / 013 / 617$ | $41 / 013 / 623$ | $\mathbf{3 . 7 / 0 . 1 2 / \mathbf { 6 3 . 8 }}$ |
| Avg. | $7.0 / 0.13 / 44.0$ | $7.4 / 0.13 / 43.5$ | $\mathbf{6 . 7 / \mathbf { 0 . 1 2 } / \mathbf { 4 6 . 1 }}$ |

Cambridge landmarks

|  |  | DUC 1 | DUC 2 |
| :---: | :--- | :---: | :---: |
| Points | HLoc | $49.0 / 69.2 / 80.3$ | $52.7 / \mathbf{7 7 . 1} / 80.9$ |
| Points | PtLine | $49.0 / 69.2 / \mathbf{8 1 . 8}$ | $56.5 / 76.3 / 80.2$ |
| + Lines | Ours | $\mathbf{4 9 . 5} / \mathbf{7 2 . 2} / 81.3$ | $\mathbf{6 0 . 3} / 76.8 / \mathbf{8 1 . 7}$ |

InLoc

| Scene | HLoc | PtLine | Ours |
| :--- | :---: | :---: | :---: |
| Chess | $\mathbf{2 . 4} / \mathbf{0 . 8 4} / \mathbf{9 3 . 0}$ | $\mathbf{2 . 4} / 0.85 / 92.7$ | $2.5 / 0.85 / 92.3$ |
| Fire | $2.3 / 0.89 / 88.9$ | $2.3 / 0.91 / 87.9$ | $\mathbf{2 . 1} / \mathbf{0 . 8 4} / \mathbf{9 5 . 5}$ |
| Heads | $\mathbf{1 . 1} / \mathbf{0 . 7 5} / \mathbf{9 5 . 9}$ | $1.2 / 0.81 / 95.2$ | $\mathbf{1 . 1} / 0.76 / \mathbf{9 5 . 9}$ |
| Office | $3.1 / 0.91 / 77.0$ | $3.2 / 0.96 / 74.5$ | $\mathbf{3 . 0} / \mathbf{0 . 8 9} / \mathbf{7 8 . 4}$ |
| Pumpkin | $5.0 / 1.32 / 50.4$ | $5.1 / 1.35 / 49.0$ | $\mathbf{4 . 7} / \mathbf{1 . 2 3} / \mathbf{5 2 . 9}$ |
| Redkitchen | $4.2 / \mathbf{1 . 3 9} / 58.9$ | $4.3 / 1.42 / 58.0$ | $\mathbf{4 . 1} / \mathbf{1 . 3 9} / \mathbf{6 0 . 2}$ |
| Stairs | $5.2 / 1.46 / 46.8$ | $4.8 / 1.33 / 51.9$ | $\mathbf{3 . 7} / \mathbf{1 . 0 2} / \mathbf{7 1 . 1}$ |
| Avg. | $3.3 / 1.08 / 73.0$ | $3.3 / 1.09 / 72.7$ | $\mathbf{3 . 0} / \mathbf{1 . 0 0} / \mathbf{7 8 . 0}$ |

7scenes RGB

| Scene | HLoc w/ Depth | PtLine | Ours w/ Depth |
| :--- | :---: | :---: | :---: |
| Chess | $\mathbf{2 . 4} / \mathbf{0 . 8 1} / 94.8$ | $\mathbf{2 . 4} / \mathbf{0 . 8 1} / \mathbf{9 5 . 0}$ | $\mathbf{2 . 4} / 0.82 / 94.0$ |
| Fire | $1.9 / 0.76 / 96.4$ | $1.9 / 0.76 / \mathbf{9 6 . 6}$ | $\mathbf{1 . 7} / \mathbf{0 . 7 1} / \mathbf{9 6 . 6}$ |
| Heads | $1.1 / 0.73 / 99.0$ | $1.1 / 0.74 / \mathbf{9 9 . 4}$ | $\mathbf{1 . 0} / \mathbf{0 . 7 2} / \mathbf{9 9 . 4}$ |
| Office | $2.7 / 0.83 / 83.7$ | $2.7 / 0.83 / 83.9$ | $\mathbf{2 . 6} / \mathbf{0 . 8 0} / \mathbf{8 4 . 7}$ |
| Pumpkin | $4.1 / \mathbf{1 . 0 5} / \mathbf{6 1 . 3}$ | $4.0 / 1.06 / 60.8$ | $\mathbf{4 . 0} / \mathbf{1 . 0 5} / 61.1$ |
| Redkitchen | $3.3 / \mathbf{1 . 1 2} / 72.1$ | $\mathbf{3 . 2} / \mathbf{1 . 1 2} / 72.5$ | $3.3 / \mathbf{1 . 1 2} / \mathbf{7 3 . 0}$ |
| Stairs | $4.7 / 1.25 / 53.4$ | $4.3 / 1.16 / 55.9$ | $\mathbf{3 . 2} / \mathbf{0 8 6} / \mathbf{7 6 . 0}$ |
| Avg. | $2.9 / 0.94 / 80.1$ | $2.8 / 0.93 / 80.6$ | $\mathbf{2 . 6} / \mathbf{0 . 8 7} / \mathbf{8 3 . 5}$ |

Consistent improvement with lines on public benchmarks

## Localization on LaMAR [A]



Large-scale 3D line maps of CAB building


Recall(\%) @ 3cm-3 ${ }^{\circ}$


Recall(\%) @ 2cm-2․


Recall(\%) @ 5cm-5 ${ }^{\circ}$

[A] Sarlin \& Dusmanu et al. LaMAR: Benchmarking Localization and Mapping for AR, ECCV 2022
Slide credits: Thomas Birchler, Shinjeong Kim, Elias Salameh, and Aidyn Ubingazhibov from ETH Zurich

## Hybrid bundle adjustment with points and lines

|  | COLMAP [42] | [42] + LIMAP (line-only) | [42] + LIMAP |
| :--- | :---: | :---: | :---: |
| ai_001_001 | $68.0 / 87.0 / 91.3$ | $78.3 / 91.1 / 93.8$ | $\mathbf{8 0 . 0} / \mathbf{9 1 . 7} / \mathbf{9 4 . 2}$ |
| ai_001_002 | $75.2 / 90.2 / 94.0$ | $87.5 / 95.6 / 97.3$ | $\mathbf{8 8 . 5} / \mathbf{9 6 . 0} / \mathbf{9 7 . 6}$ |
| ai_001_003 | $83.8 / 94.4 / 96.6$ | $82.9 / 94.0 / 96.4$ | $\mathbf{8 5 . 7} / \mathbf{9 5 . 1} / \mathbf{9 7 . 1}$ |
| ai_001_004 | $\mathbf{7 9 . 2} / \mathbf{8 8 . 9 / 9 0 . 9}$ | $67.1 / 82.1 / 86.0$ | $77.3 / 88.3 / 90.6$ |
| ai_001_005 | $85.1 / 94.9 / 97.0$ | $88.4 / 96.1 / 97.7$ | $\mathbf{9 0 . 9 / \mathbf { 9 7 . 0 } / \mathbf { 9 8 . 2 }}$ |
| ai_001_006 | $83.4 / 93.1 / 95.7$ | $80.2 / 92.9 / 95.7$ | $\mathbf{8 4 . 4} / \mathbf{9 3 . 8} / \mathbf{9 6 . 3}$ |
| ai_001_007 | $59.0 / 68.5 / 70.6$ | $64.5 / \mathbf{7 0 . 6} / \mathbf{7 1 . 9}$ | $\mathbf{6 5 . 0} / 70.3 / 7.7$ |
| ai_001_008 | $84.9 / 94.9 / 96.9$ | $89.5 / 96.5 / 97.9$ | $\mathbf{9 1 . 3} / \mathbf{9 7 . 1} / \mathbf{9 8 . 2}$ |
| Average $\uparrow$ | $77.3 / 89.0 / 91.6$ | $79.8 / 89.9 / 92.1$ | $\mathbf{8 2 . 9} / \mathbf{9 1 . 2} / \mathbf{9 3 . 0}$ |
| Median error $\downarrow$ | 0.188 | 0.173 | $\mathbf{0 . 1 4 6}$ |

## Line-assisted multi-view stereo


w. Line-based Energy

Preliminary line-assisted dense mapping.

## Featuremetric Line Refinement

Sampling by 2-level intersection!

a) Reference image

b) Feature map

c) Target image

d) Correspondences

Line patching with oriented bounding box to ensure scalability

## Benchmarking

|  | Detector | LSD | HAWPv3 | TP-LSD | DeepLSD |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Matcher |  |  |  |  |  |
| LBD | $42.2 / 58.5 /(14.0 / 14.6)$ | $6.0 / 58.0 /(7.8 / 9.8)$ | $21.6 / 73.2 /(9.1 / 9.3)$ | $30.7 / 69.3 /(12.2 / 18.7)$ | $64.6 / 70.0 /(15.8 / 18.1)$ |
| SOLD2 | $48.3 / 59.2 /(15.8 / 19.1)$ | $14.7 / 62.7 /(11.2 / 20.1)$ | $44.4 / 76.4 /(14.3 / 16.7)$ | $50.8 / 74.4 /(15.1 / 32.2)$ | $72.0 / 71.4 /(18.1 / 24.9)$ |
| L2D2 | $44.4 / 59.6 /(15.0 / 16.8)$ | $13.5 / 63.4 /(10.7 / 18.3)$ | $39.5 / 78.1 /(13.7 / 15.4)$ | $43.9 / 72.8 /(13.7 / 24.9)$ | $69.2 / 70.4 /(17.0 / 22.2)$ |
| LineTR | $37.0 / 58.3 /(12.8 / 13.3)$ | $5.4 / 60.5 /(8.4 / 10.7)$ | $43.0 / 76.3 /(14.5 / 16.7)$ | $29.0 / 70.1 /(12.3 / 19.9)$ | $71.9 / 69.4 /(17.6 / 23.9)$ |
| Endpts SP + NN |  | $48.8 / 58.6 /(15.5 / 18.2)$ | $16.2 / 63.2 /(11.2 / 20.0)$ | $43.7 / 75.8 /(14.3 / 16.5)$ | $49.1 / 73.7 /(14.7 / 31.4)$ |
| Endpts SP + SG |  | $48.4 / 58.0 /(15.8 / 18.9)$ | $16.0 / 61.9 /(11.3 / 20.9)$ | $47.1 / 76.1 /(14.5 / 16.8)$ | $50.0 / 72.8 /(15.5 / \mathbf{3 4 . 4})$ |

Pautrat et al. DeepLSD: Line Segment Detection and Refinement with Deep Image Gradients, CVPR 2023

Next Step: Hybrid Incremental SfM

## 3D Line Mapping Revisited ${ }_{\text {smummen }}$

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